

Homework2

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1 Armijo Gradient

$$f(x) = x^2 \exp(-x) - x$$

$$x_0 = 0.5 \text{ and } x_0 = 2$$

To calculate Armijo gradient algorithm, I've assumed α as a random number between 0 and 1.

Step 1. Compute the Descent Direction

$$h_i = h(x_i) = -\nabla f(x_i)$$

Stop if $\nabla f(x_i) = 0$

$$\nabla f(x) = -x^2 \exp(-x) + 2 \exp(-x)x - 1$$

Step 2. Compute the step size

Find the max argument of α_m , set it as λ

$$f(x_k + \alpha_m d_k) \leq f(x_k) + \alpha_m \beta \nabla f(x_k)^T d_k$$

$\lambda \in (0, 2(1 - \alpha/M))$ where M is larger than Double differential of f(x).

Step 3. Update x

$$x_{i+1} = x_i + \lambda h_i$$

and go back to step 1.

$$f(x_k + \alpha_m d_k) \leq f(x_k) + \alpha_m \beta \nabla f(x_k)^T d_k$$

$$\leq \lambda \|\nabla f(x_i)\|^2 \|(M/2\lambda - (1 - \alpha))\|$$

by mean value Theorem

$$\lambda \in (0, 2(1 - \alpha)/M)$$

To calculate armijo gradient algorithm when $x_0 = 0.5$, h_0 becomes -0.5451.

$$[h_1, h_2, h_3, \dots] = [-0.02001627842295628, -2.658723154969067e-07, -1.3633538742396922e-12, 0.0, 0.0, \dots]$$

Eventually, h_i converges to be 0.

When $x_0 = 2$,

$$[h_1, h_2, h_3, \dots] = [-5.0693825587533325, -3.5393665775984573e-07, -1.5543122344752192, 0.0, 0.0, \dots]$$

Eventually, h_i converges to be 0.